# SpecTRe-GS: Modeling Highly Specular Surfaces with Reflected Nearby Objects by Tracing Rays in 3D Gaussian Splatting

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Figure 1. Our SpecTRe-GS effectively captures the appearance of reflectors with highly specular surfaces, even in the presence of nearby objects. In the real-world scene shown above, it performs favorably against previous methods [13, 15, 30, 39, 42], both visually (as the highlighted reflections within the insets) and quantitatively (with PSNR values within the reflective region annotated in the corners).

#### Abstract

3D Gaussian Splatting (3DGS), a recently emerged multiview 3D reconstruction technique, has shown significant advantages in real-time rendering and explicit editing. However, 3DGS encounters challenges in the accurate modeling of both high-frequency view-dependent appearances and global illumination effects, including inter-reflection. This paper introduces **SpecTRe-GS**, which addresses these challenges and models highly **Spec**ular surfaces that reflect nearby objects through Tracing Rays in 3D Gaussian Splatting. SpecTRe-GS separately models reflections from highly specular and rough surfaces to leverage the distinctions between their reflective properties and integrates an efficient ray tracer within the 3DGS framework for querying secondary rays, thus achieving fast and accurate rendering. Also, it incorporates normal prior guidance and joint geometry optimization at various stages of the training process to enhance geometry reconstruction for undistorted reflections. Experiments on both synthetic and real-world scenes demonstrate the superiority of SpecTRe-GS compared to existing 3DGS-based methods in capturing highly specular inter-reflections and also showcase its editing applications.

#### **1. Introduction**

Recently, 3D Gaussian Splatting (3DGS) [15] has emerged as an innovative paradigm for multi-view 3D reconstruction. Unlike its predecessor, neural radiance fields (NeRF) [23], 3DGS adopts an explicit point-based scene representation with tile-based rasterization rather than relying on ray casting through an implicit neural field for rendering. This transition endows 3DGS with significant advantages in terms of real-time rendering speed and allows for convenient post-reconstruction editing. Nevertheless, challenges arise when the scene to be reconstructed includes highly specular (i.e., mirror-like) surfaces which exhibit strong and high-frequency view-dependent appearances. The original 3DGS struggles to accurately model such high-frequency reflections, as it utilizes per-Gaussian third-order spherical harmonics (SH) to represent viewdependent appearances. This approach is restricted to lowfrequency radiance variations in angular space and is susceptible to overfitting when the training views that observe the Gaussian are not sufficiently dense [17, 37].

To address this issue, a natural strategy is to adopt a physically-based shading model and optimize reflective properties for each Gaussian [2, 7, 8, 10, 11, 13, 18, 29, 35, 36, 39, 40, 43, 47], rather than merely recording the out-

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going radiance. This strategy enables the computation of reflected radiance by evaluating the physically constrained rendering equation [14], taking into account local scene components including geometry, material properties, and incident lighting, thereby yielding more accurate, realistic, and reliable view-dependent effects. Among the three local scene components, addressing local incident lighting is perhaps the most intricate. Adopting a suboptimal approach to addressing local incident lighting may undermine global illumination effects such as inter-reflections, resulting in an unrealistic scene appearance. Notably, this issue is particularly pronounced in scenes characterized by highly specular surfaces; for instance, the absence of reflections of nearby objects would be especially noticeable. Therefore, it is crucial for methods aimed at modeling such high-frequency view-dependent appearances through the rendering equation to carefully address local incident lighting.

Unfortunately, effectively acquiring local incident lighting poses a substantial challenge for 3DGS-based methods. The advantages of 3DGS come with a trade-off: The exclusive reliance on the tile-based rasterizer limits its ability to efficiently render secondary rays emanating from vastly different origins towards arbitrary directions, which is essential for querying local incident lighting. As a compromise, a majority of methods neglect secondary effects [36, 39, 47] or periodically bake secondary effects including local occlusions [8, 40] and incident radiance [18, 29] as low-order SH stored in Gaussians or probes. However, low-order SH can only capture low-frequency variations in incident lighting, and the requirement of baking not only incurs additional storage costs but also hinders post-reconstruction editing, such as inserting or deleting nearby objects or relighting. Employing screen space ray tracing (SSRT) [2] produces high-frequency but incomplete inter-reflections as SSRT struggles to trace out-of-screen and occluded rays.

We propose SpecTRe-GS to model highly Specular surfaces with reflected nearby objects through Tracing Rays in the 3D space within the Gaussian Splatting framework, overcoming the aforementioned challenges. We first made the observation that, although highly specular surfaces exhibit reflections that can be extremely high-frequency and thus hard to capture using SH color or neural network, they are also favorable for modeling in the sense that the specular lobe of their bidirectional reflectance distribution functions (BRDF) are highly concentrated. This fact facilitates the evaluation of the rendering equation [14] on these surfaces because tracing only a few secondary rays already suffices, in contrast to rougher surfaces with more scattered specular lobes. To make use of this fact, we separately model highly specular and rough surfaces, ray-tracing the appearance of the former while retaining the low-order SH color to wellapproximate the latter, significantly reducing the amount of secondary rays to trace. To further speed up the timeconsuming ray tracing process, we implement a ray tracer within the 3DGS framework, inspired by the recent progresses [24, 42]. We also propose a training strategy to enhance the scene geometry reconstruction, the quality of which directly decides the quality of the reconstructed reflection. To summarize, our contributions are as follows:

- proposing a shading model tailored for indirect mirror reflections combined with an efficient ray tracer for fast and accurate rendering;
- designing a training strategy to enhance geometry reconstruction for precise incident direction computing; and
- achieving state-of-the-art novel view synthesis results on scenes with highly specular reflections (shown in Fig. 1).

## 2. Related Work

Improving view-dependent appearances in 3DGS. The original 3DGS [15] uses low-order SH color that captures only low-frequency angular variations, a limitation that many follow-up methods were trying to address (see Tab. 1). While a few methods [30, 35] (row 2) adopt neural networks to decode local features, the majority [2, 8, 10, 13, 18, 29, 36, 39, 40, 47] (rows 3-8) employ the physicallybased rendering equation [14]. This equation offers the most accurate approach for modeling view-dependent appearances but requires explicit modeling of surface normals, BRDFs, and the most demanding component - incident lighting. The rendering equation can accommodate all-frequency BRDFs; thus, the frequency of the reflected radiance is now bounded by that of the modeled incident lighting. While an environment map suffices to model direct lighting, it is significantly more challenging to model indirect lighting responsible for global illumination effects including occlusions and inter-reflections. Some methods circumvent this issue by ignoring secondary effects [36] (row 3) or by using a residual color [13] (row 4). For methods that explicitly model indirect lighting, a common strategy is to periodically bake occlusions [8] or interreflections [18, 29] into low-order SH, thereby limiting their incident radiance to low-frequency variations (rows 5-7). GI-GS [2] (row 8) uses screen space ray tracing to simulate high-frequency inter-reflections; however, it only models those whose sources are directly visible in the viewport. There are also specialized methods for plane mirrors that reflect the point cloud or camera about the plane [19, 22]. Our SpecTRe-GS traces the incident lighting in 3D space, thus is able to render high-frequency and complete interreflections for highly specular surfaces with convex shapes. Ray-based 3D Gaussian rendering. It is noteworthy that tracing secondary rays for incoming local lighting has almost become a common practice in recent NeRF-based methods that explicitly model specular reflections or interreflections [9, 20, 32, 33, 45]. However, it is challenging to achieve this in 3DGS-based frameworks. 3DGRT [24]

Table 1. We summarize works improving the view-dependent appearances upon 3DGS [15] based on: How do they model the view-dependent appearances (*i.e.*, the outgoing radiance) and the supported frequency in angular space; how do they accommodate the global illumination effects (*i.e.*, the local incident lighting) including occlusions and inter-reflections and the supported frequency in angular space; and whether is it feasible to edit the scene appearance under (in)direct lighting after reconstruction without any re-baking.

Method	View-dependent Appearance		Global II	Editable			
Method	Modeling	Frequency	Occlusion	Occlusion Inter-reflection		Appearance	
(1) 3DGS [15]	Low-order SH	Low	Jointly baked in outgoing SH color		Low	None	
(2) 3iGS [30]; [35]	Neural network	Netbounded	Jointly baked in the neural feature		Netbounded	None	
(3) DeferredGS [36]			Ignored		None		
(4) GShader [13]; [39]		Arbitrary, thus	Jointly baked in outgoi				
(5) GS-ID [8]; [40]	Physically-	bounded	Dalas I as CII	Ignored		Direct	
(6) GS-IR [18]; [10]	based rendering	by the frequency	Baked as SH	Baked as SH	Low		
(7) GIR [29]	equation [14]	of	Ray-traced in 3D space	Baked as SH			
(8) GI-GS [2]		lighting	Ray-traced in screen spa	Ray-traced in screen space, incomplete			
(9) Ours		0.0	Ray-traced in 3	D space	High	(In)direct	

first demonstrates efficient ray tracing in 3D Gaussians, enabling ray-based lighting effects such as non-projective views. RayGauss [1] and EVER [21] employ ray sampling in 3D Gaussians, mitigating common artifacts in 3DGS, such as aliasing [41], popping artifacts [27] and projection errors [12]. Yang *et al.* [46] adopt path tracing to simulate global illumination with Gaussian primitives. Meanwhile, Jorge *et al.* [4] utilizes ray sampling to simulate volumetric scattering and emissive media. Our SpecTRe-GS integrates ray tracing techniques to evaluate accurate incident radiance in the 3DGS framework at an affordable cost.

# 3. Proposed Method

Our method is specifically designed to accurately model the high-frequency reflections of highly specular surfaces. We build upon the recent advancements in 3DGS (Sec. 3.1) and adapt the reflection model to efficiently handle scenes comprising both highly specular objects and rougher objects (Sec. 3.2). To precisely and reliably query the incident radiance necessary for rendering both direct and indirect highly specular reflections, we incorporate ray tracing within the 3DGS framework (Sec. 3.3). We employ a dedicated training strategy to enhance geometry reconstruction, which is crucial for rendering undistorted and realistic reflections (Sec. 3.4). Our pipeline is outlined in Fig. 2.

## 3.1. Preliminary

The seminal work of 3DGS [15] represents the scene as a translucent Gaussian point cloud, where each 3D Gaussian is described with central point  $\mu \in \mathbb{R}^3$ , scales  $s \in \mathbb{R}^3$ , rotation quaternion  $q \in \mathbb{R}^4$ , and opacity  $\sigma \in [0, 1]$ . The distribution of each Gaussian in 3D space is given by  $G(\mathbf{x}) = e^{-\frac{1}{2}(\mathbf{x}-\mu)^\top \Sigma^{-1}(\mathbf{x}-\mu)}$ , where the covariance  $\Sigma = \mathbf{RSS}^\top \mathbf{R}^\top$  is compactly parameterized as s and q. By performing local affine transformation [48], 3D Gaussians are projected as 2D Gaussians on the image plane for rasterization. Then for each ray corresponding to an image pixel, the contributing 2D Gaussians are accumulated from front to back for volumetric rendering:

$$I(\boldsymbol{\omega}_{\mathrm{o}}) = \sum_{i} \boldsymbol{c}_{i}(\boldsymbol{\omega}_{\mathrm{o}}) \alpha_{i} \prod_{j=1}^{i-1} (1 - \alpha_{j}), \qquad (1)$$

where  $\alpha_i = \sigma_i G_i$  and the view-dependent color  $c_i(\omega_0) \in \mathbb{R}^3$  is modeled by third-order SH coefficients  $\varphi_i \in \mathbb{R}^{48}$ .

Besides the view-dependent color  $c_i$ , many other optimizable attributes including surface normal, diffuse albedo, or occlusion information, can be attached to each Gaussian. These attributes can be used locally in each Gaussian, or be accumulated to a map in the same way as Eq. (1) for later applications such as deferred shading [39].

#### 3.2. Highly Specular Reflection Modeling

To model high-frequency reflections, we follow the convention to incorporate the physically-based rendering equation [14]. As commonly observed phenomena in realworld life, the inter-reflections from the nearby objects on highly specular surfaces should be modeled for a photorealistic scene appearance. The common practice with distant environment maps [13] ignores such inter-reflections and does not suffice for this task, thus we employ raytracing (detailed in Sec. 3.3) in 3D space for a complete and high-frequency inter-reflection. However, we found that performing ray tracing on the entire scene, including highly specular surfaces and rougher surfaces, is highly time-consuming. Evaluating the rendering equation [14] on rougher surfaces typically needs larger samples of the incident lighting even with multiple importance sampling [31], thus heavily increases the computational cost. Fortunately, previous works [15] have proven that rough surfaces can be well-captured by directly optimizing the outgoing color. Therefore, we propose the following reflection model that treats highly specular surfaces and rougher surfaces sepa-



Figure 2. Overview of the SpecTRe-GS pipeline. The scene is represented as a Gaussian point cloud, where each Gaussian is associated with geometry and shading attributes used to render the depth map D, normal map N, diffuse reflection  $I_{\text{diff}}$ , specular reflectance  $A_{\text{spec}}$ , and rough surface reflection  $I_{\text{rs}}$  through splatting (Sec. 3.1). Highly specular surface reflection  $I_{\text{ss}}$  is formulated as the sum of the diffuse reflection  $I_{\text{diff}}$  and the specular reflection computed from the incident radiance  $I_i$  and specular reflectance  $A_{\text{spec}}$  (Sec. 3.2). The incident radiance  $I_i$  is determined along reflected secondary rays given by the scene geometry D and N, with the indirect component  $I_{\text{ind}}$  and visibility  $V_i$  evaluated via efficient ray tracing within the Gaussian point cloud, and the direct component  $I_{\text{dir}}$  modeled by an optimizable environment map (Sec. 3.3). The scene geometry is enhanced using normal prior guidance, numerical gradients from ray-traced incident radiance, and other training signals to achieve undistorted reflections (Sec. 3.4).

rately to enhance the specular reflections while maintaining the rendering speed. Also, we follow deferred shading [5] to shade for each pixel instead of each Gaussian, as it reduces the computation and gives sharp surface normals [47].

**Modeling highly specular surfaces.** To model surfaces that may exhibit both highly specular and diffuse reflections, such as polished marble, we define the reflection  $I_{ss}$  for these highly specular surfaces at surface point x, observed from view direction  $\omega_0$  as follows:

$$I_{\rm ss}(\boldsymbol{x}, \boldsymbol{\omega}_{\rm o}) = I_{\rm diff}(\boldsymbol{x}) + I_{\rm spec}(\boldsymbol{x}, \boldsymbol{\omega}_{\rm o}).$$
 (2)

While the diffuse reflection  $I_{\text{diff}}$  is the view-independent outgoing radiance directly optimized as d in each Gaussian, the specular reflection  $I_{\text{spec}}$  is approximated with an ideal mirror reflection:

$$I_{\rm spec}(\boldsymbol{x}, \boldsymbol{\omega}_{\rm o}) = A_{\rm spec}(\boldsymbol{x}, \boldsymbol{\omega}_{\rm r}) I_{\rm i}(\boldsymbol{x}, \boldsymbol{\omega}_{\rm r}),$$
 (3)

where the reflected incident direction  $\omega_r$  is given by  $\omega_o - 2\omega_o^{\top} \boldsymbol{n} \cdot \boldsymbol{n}$  in which  $\boldsymbol{n}$  denotes the local surface normal, and  $A_{\text{spec}}$  is the specular reflectance considering Fresnel effects through Schlick's approximation [28]<sup>1</sup>:

$$A_{\text{spec}}(\boldsymbol{x},\boldsymbol{\omega}_{\text{r}}) = F_0(\boldsymbol{x}) + (1 - F_0(\boldsymbol{x}))(1 - \boldsymbol{n}^\top \boldsymbol{\omega}_{\text{r}})^5.$$
(4)

Here,  $F_0$  is the specular reflectance at normal incidence optimized as  $f_0$  in each Gaussian and is 3-channel to support metallic materials. The incident radiance  $I_i$  in  $\omega_r$  originates from both direct and indirect sources:

$$M_{
m i}(oldsymbol{x},oldsymbol{\omega}_{
m r}) = V_{
m i}(oldsymbol{x},oldsymbol{\omega}_{
m r}) I_{
m dir}(oldsymbol{\omega}_{
m r}) + (1-V_{
m i}(oldsymbol{x},oldsymbol{\omega}_{
m r})) I_{
m ind}(oldsymbol{x},oldsymbol{\omega}_{
m r})$$

(5)

where  $V_i \in [0, 1]$  quantifies the proportion of the incident lighting occluded by the scene itself,  $I_{dir}$  is the direct incident lighting from a distant environment map, and  $I_{ind}$  is the indirect incident radiance from the scene.

**Defining depth and surface normal of Gaussians.** It is essential to accurately acquire the depth and surface normal of each Gaussian in our method, as they directly determine the origin and direction of the reflection. However, they are ambiguous because the Gaussians are translucent ellipsoids in 3D space. Instead of treating the depth of the projected center and the shortest axis direction facing the camera as the depth and normal of each Gaussian [13, 17, 39], we adopt the formulation in GOF [42] to calculate for each Gaussian the "intersection point" along the ray achieving the maximum response, using its depth and normal of the intersection plane. This formulation gives a better and more consistent geometry reconstruction with 3D Gaussians.

**Modeling the whole image.** We model the part of the scene containing highly specular surfaces using Eq. (2). For the other part which exhibits only low-frequency view dependencies, we follow GOF [42] to model the appearance  $I_{\rm rs}$  of the rougher surfaces using per-Gaussian SH coefficients  $\varphi$ . We combine  $I_{\rm ss}$  and  $I_{\rm rs}$  using a binary mask M (which can be handily acquired through pre-trained segmentation models such as SAM [16]) specifying the highly specular

<sup>&</sup>lt;sup>1</sup>We omit the distribution and mask-shadowing term in the microfacet model as we assume ideal mirror reflection.

surfaces within the scene ( $\odot$  is pixel-wise multiplication):

$$I(\boldsymbol{\omega}_{\rm o}) = I_{\rm ss}(\boldsymbol{\omega}_{\rm o}) \odot M + I_{\rm rs}(\boldsymbol{\omega}_{\rm o}) \odot (1 - M).$$
(6)

## 3.3. Efficient Ray Tracing for Incident Radiance

To accurately compute the reflection from highly specular surfaces, it is crucial to obtain the incident radiance at the reflected view direction as modeled by Eq. (5), which incorporates both direct and indirect lighting. However, due to the incoherent origins and directions of these secondary rays, the incident radiance cannot be efficiently rendered using the rasterizer from the original 3DGS [15], as it relies on the locality of the rays, nor can it be computed merely using an environment map, which considers only direct lighting [13]. Inspired by the recent work 3DGRT [24], we implement an efficient ray tracer within the 3DGS framework to compute the radiance of secondary rays, thus achieving high-frequency and accurate reflections.

Geometry acceleration structure (GAS). For fast scene traversal, we construct a GAS within the OptiX programming interface [25], which uses ray tracing hardware to accelerate ray-primitive intersection tests and is several times faster than BVH [3] in CUDA. Instead of using axis-aligned bounding boxes which inefficiently encapsulate irregular Gaussians and lead to false positives, we adopt stretched icosahedrons as proxy meshes for more efficient ray intersection [24]. The vertex j of the icosahedron approximating Gaussian i is given by:

$$\boldsymbol{v}_{i,j} = \sqrt{2\log\left(\sigma_i/\alpha_{\min}\right)} \mathbf{R}_i^{\top} \mathbf{S}_i^{\top} \boldsymbol{v}_j^{\text{unit}} + \boldsymbol{\mu}_i, \qquad (7)$$

where  $v_j^{\text{unit}}$  is the vertex of an inscribed icosahedron in a unit sphere. Here,  $\alpha_{\min}$  serves as a threshold that adaptively scales each icosahedron by dictating the minimal contribution of the Gaussian at the transformed vertices, thereby reducing the computational overhead during intersection and radiance evaluation. We regularly update the GAS after each densification operation [15] and every  $n_{\text{up}}$  step as the Gaussian point cloud changes along the training.

**Ray queries with GAS.** To evaluate the incident radiance  $I_{ind}(\boldsymbol{x}_0, \boldsymbol{\omega}_r)$ , secondary rays  $\boldsymbol{x}(t) = \boldsymbol{x}_0 + t\boldsymbol{\omega}_r$  are traced against proxy meshes within the GAS. Upon tracing each ray, we first collect the *k* closest valid hits, each corresponding to a Gaussian with  $\alpha_i \geq \alpha_{min}$ . The depth of the "true" intersection point for each Gaussian is defined as:

$$t_{\max,i} = \frac{(\boldsymbol{\mu}_i - \boldsymbol{x}_0)^\top \boldsymbol{\Sigma}_i^{-1} \boldsymbol{\omega}_{\mathrm{r}}}{\boldsymbol{\omega}_{\mathrm{r}}^\top \boldsymbol{\Sigma}_i^{-1} \boldsymbol{\omega}_{\mathrm{r}}},\tag{8}$$

which maximizes the Gaussian's contribution  $\sigma_i G_i(\mathbf{x}_0 + t_{\max,i}\omega_r)$ . We then sort the Gaussians by their depth and update the ray depth  $D_{\text{ind}}$ , visibility (*i.e.*, transmittance)  $V_i$ , and color  $I_{\text{ind}}$  (using the Gaussians' outgoing SH colors assuming that they model rough surfaces), following Eq. (1). The above process is repeated after advancing the ray origin until no more valid hits remain or the ray transmittance

drops below a threshold. For the transmittance that remains unoccluded by the reconstructed scene itself, we adopt an optimizable environment map for calculating the direct incident radiance  $I_{dir}(\omega)$ . According to Eq. (5), the final incident radiance  $I_i(\boldsymbol{x}, \omega_r)$  combines direct and indirect components, weighted by visibility  $V_i(\boldsymbol{x}, \omega)$ .

Thanks to the efficient and hardware-accelerated ray tracing techniques elaborated above, as well as our separate modeling of highly specular and rough surfaces, the average rendering time of our method is only 50% to 100% slower than that of a pure rasterizer on each of our test scenes. This varies according to the density of objects in the scene and the proportion of highly specular surfaces.

#### 3.4. Training

We propose a training strategy that especially focuses on enhancing the geometry reconstruction, as unfaithful scene geometry induces inaccurate secondary rays and results in distorted reflections. We optimize our model from an initial sparse point cloud using the following loss terms:

$$\mathcal{L} = \mathcal{L}_{c} + \lambda_{d} \mathcal{L}_{d} + \lambda_{dn} \mathcal{L}_{dn} + \lambda_{sm} \mathcal{L}_{sm} + \lambda_{n} \mathcal{L}_{n} + \lambda_{r} \mathcal{L}_{r}, \quad (9)$$

where  $\mathcal{L}_c$  is a color reconstruction loss [15] differentiable to the geometry,  $\mathcal{L}_d$  and  $\mathcal{L}_{dn}$  are the distortion and depthnormal consistency loss used in GOF [42],  $\mathcal{L}_{sm}$  is an edgeaware smoothness term for the normal and specular reflectance for the highly specular surfaces,  $\mathcal{L}_n$  is a normal prior term to employ data-driven clues, and  $\mathcal{L}_r$  is a residualsuppressing term for progressive learning. This section describes these terms and more details are in the supplement. **Normal prior guidance.** To tackle the challenging problem of reconstructing geometry for highly specular objects, we employ StableNormal [38] to provide monocular normal priors  $\hat{N}$ , offering initial geometric constraints:

$$\mathcal{L}_{n} = 1/|N| \sum ||(\hat{N} - N) \odot M||_{1}.$$
 (10)

**Joint geometry optimization.** Recognizing potential inaccuracies and inconsistencies across views in the normal prior, we concurrently optimize the scene geometry during training. This is achieved by differentiating the incident radiance  $I_i$ , which relates to the final image through Eq. (2) and Eq. (3), with respect to the scene geometry. Computing the gradient of the direct incident radiance  $I_{dir}$  is straightforward. To compute the gradient of the indirect incident radiance  $I_{ind}$  concerning the local surface normal n, we adopt a simple yet effective finite difference method to numerically evaluate the gradient of  $I_{ind}$  with respect to the reflected direction  $\omega$  that depends on n:

$$\frac{\partial I_{\text{ind}}}{\partial \omega^{i}} \bigg|_{\omega_{0}} \approx \frac{I_{\text{ind}}(\boldsymbol{x}, \omega_{0} + \Delta_{\boldsymbol{\omega}}^{i}) - I_{\text{ind}}(\boldsymbol{x}, \omega_{0} - \Delta_{\boldsymbol{\omega}}^{i})}{2\Delta_{\boldsymbol{\omega}}^{i}}, \quad (11)$$

where  $\Delta_{\omega}^{i}$  denotes the perturbation of the *i*-th dimension in  $\omega$ . Considering that using the same perturbation for sec-

Table 2. Quantitative comparisons of novel view synthesis results with state-of-the-art methods on both synthetic and real-world scenes. We report the scores of PSNR, SSIM [34], and LPIPS [44] for entire images and within reflective regions.  $\uparrow(\downarrow)$  means higher (lower) is better. We mark the **best** and the <u>second best</u> results in each column.

Data	Synthe	etic (entire	image)	Synt	hetic (refle	ctive)	Real-w	orld (entire	e image)	Real-	world (refle	ective)
Method	<b>PSNR</b> ↑	SSIM↑	LPIPS↓	<b>PSNR</b> ↑	SSIM↑	LPIPS↓	<b>PSNR</b> ↑	SSIM↑	LPIPS↓	<b>PSNR</b> ↑	SSIM↑	LPIPS↓
3DGS [15]	27.71	0.910	0.131	21.51	0.940	0.078	24.82	0.823	0.227	21.31	0.965	0.047
GOF [42]	27.97	0.917	0.117	21.38	0.940	0.076	24.86	0.826	0.219	21.25	0.963	0.047
GOF* [42]	27.57	0.913	0.125	20.67	0.936	0.085	24.69	0.825	0.223	20.44	0.962	0.051
3iGS [30]	28.58	0.912	0.125	21.98	0.939	0.076	24.37	0.809	0.233	21.22	0.963	0.048
GShader [13]	26.65	0.888	0.160	20.79	0.935	0.086	23.93	0.810	0.255	20.23	0.963	0.053
GShader* [13]	27.14	0.894	0.153	21.22	0.938	0.084	24.03	0.812	0.253	20.36	0.964	0.053
3DGS-DR [39]	27.62	0.890	0.173	21.57	0.938	0.085	24.79	0.824	0.243	21.18	0.965	0.050
3DGS-DR* [39]	26.97	0.883	0.182	21.18	0.936	0.088	24.60	0.823	0.251	20.38	0.964	0.055
Ours	29.41	0.922	0.109	23.28	0.949	0.062	25.11	0.828	0.213	22.77	0.967	0.035

ondary rays with different depths  $D_{ind}$  leads to different amounts of intersection movements, making the numerical gradient less accurate, we use a depth-aware ray perturbation that adjusts to  $D_{ind}$  for more informative gradients:

$$\Delta_{\boldsymbol{\omega}}^{i} = \theta_{\rm d} \max(\min(D_{\rm ind}/D_0, \sigma_{\rm d}^{\rm max}), \sigma_{\rm d}^{\rm min}), \qquad (12)$$

where  $\theta_d$  and  $D_0$  define a reference angular perturbation and  $\sigma_d^{\min}$  and  $\sigma_d^{\max}$  ensure numerical stability. For computational efficiency, we disregard the gradient with respect to the point position p, as we find reflections are distorted mainly due to normal errors. We detach visibility  $V_{ind}$  and depth  $D_{ind}$  because the sparsity of the visibility gradient and abrupt changes in depth damage numerical stability.

**Progressive learning.** As training progresses, monocular normal priors may hinder the accurate geometry reconstruction, thus we gradually decay the weight of normal prior guidance  $\lambda_n$ , letting gradients from physics-based rendering take over the fine-tuning of scene geometry. Besides, for smoother training and consequently better reconstruction within the reflective regions, we replace the hard mask M used in Eq. (6) with a relaxed version  $1 - I_r$  rendered with another per-Gaussian attribute  $r \in [0, 1]$  using Eq. (1). We encourage the reflective region to be modeled with highly specular reflections by suppressing the residual within M:

$$\mathcal{L}_{\rm r} = 1/|M| \sum ||I_{\rm r} \odot M||_1.$$
 (13)

# 4. Experiments

In this section, we compare our method on both synthetic and real-world scenes (Sec. 4.2) against state-of-the-art methods (Sec. 4.3). We also perform ablation studies to validate the key components of our method (Sec. 4.4) and explore applications in scene editing (Sec. 4.5). Please check the supplementary material for more implementation details, data creation details, and experimental results.

### **4.1. Implementation Details**

We implement our method in PyTorch [26] with CUDA kernels for rasterization based on GOF [42] and custom OptiX programs for ray tracing. We conduct all experiments on a GPU with 24 GB VRAM, 83 shader core TFLOPS, and 191 ray tracing core TFLOPS. We set  $\lambda_{\rm sm} = 0.5$ ,  $\lambda_{\rm r} = 1.0$ , and  $\lambda_{\rm n} = 0.5$ , exponentially decaying to 0.0025 from 4k to 10k iterations. We use r = 0.9 as the initialization. For other hyperparameters, we use the settings in GOF [42].

#### 4.2. Datasets

Synthetic scenes. We build 6 synthetic scenes, each containing multiple surrounding objects and a highly specular surface with distinctive properties: HELMET, MAR-BLETABLE, VASE, POT, TOASTER, and MIRROR. For each scene, we use the Blender Cycles engine [6] to render about 300 images of resolution  $1024 \times 1024$ , of which 2/3 are used for training and the rest are left for testing.

**Real-world scenes.** For real-world validation, we capture two scenes: REALBOWL and REALPOT, consisting of 138 and 139 images of resolution  $1440 \times 1080$  respectively, with every eighth image reserved in the test set.

#### 4.3. Comparison

**Comparing methods.** We compare our method with 5 open-source state-of-the-art methods: the original 3DGS [15]; GOF [42] which focus on geometry reconstruction with 3D Gaussians; 3iGS [30] which improves view-dependent effects through neural features; and 3DGS-DR [39] and GShader [13] which are adapted for specular reflection employing physically-based rendering (PBR). For a fair comparison, we provide GOF [42], 3DGS-DR [39], and GShader [13] with the normal prior guidance, and indicate these versions by "\*" throughout this paper. **Evaluation protocol.** We report peak signal-to-noise ratio (PSNR), structural similarity index measure (SSIM) [34], and learned perceptual image patch similarity (LPIPS) [44] measured on both entire images and reflective regions.

**Quantitative evaluation.** As shown in Tab. 2, our method outperforms comparing methods on both synthetic and real-world scenes, especially in reflective regions. It is worth noting that using normal prior guidance usually leads to degradation of GOF [42] which relies solely on SH color, as it suppresses the ability to simulate high-frequency appear-



Figure 3. Novel view synthesis comparison on synthetic scenes. We evaluate SpecTRe-GS against relevant 3DGS-based methods modeling view-dependent appearances: 3DGS-DR [39], GShader [13], 3iGS [30], GOF [42], and 3DGS [15]. The insets highlight the improvement of SpecTRe-GS in rendering high-frequency specular reflections, showcasing the precise positioning of reflected content and sharp details.



Figure 4. Novel view synthesis and image decomposition results on synthetic scenes, comparing our SpecTRe-GS with 3DGS-DR [39] and GShader [13]. SpecTRe-GS better distinguishes diffuse and specular components in reflective regions, with the least baked-in view-dependent appearance in diffuse components. The masks of reflective regions are shown as insets in the reference image.

ances through false geometry. In contrast, the influence of this guidance on 3DGS-DR [39] and GShader [13] is two-fold: It facilitates the reconstruction of appearance under direct lighting, but also prevents these methods from imitating specular inter-reflections by faking geometry.

**Qualitative evaluation.** In visual comparisons, we show results of GOF [42], GShader\* [13], and 3DGS-DR [39] as they are variants with higher qualities. As shown in Fig. 3, our method performs better than the baseline methods for both planar reflectors (rows 1-2) and curved reflectors (row 3), capturing clean, accurate, and high-frequency specular

reflections. Our method also surpasses baseline methods in real-world scenes, as shown in Fig. 1. By visualizing the separate components of PBR-based methods in Fig. 4, we find that incident radiance modeling for both direct and indirect sources is vital for physically meaningful scene appearance decomposition. Otherwise, to fit the overall color in training images, indirect incident radiance is heavily baked into the diffuse component (row 1 for 3DGS-DR [39] and row 3 for GShader [13]). The baked-in incident radiance loses high-frequency details and prevents realistic scene editing in a physically-accurate manner. It should be noted



Figure 5. Our reconstruction results on two real-world scenes. SpecTRe-GS accurately reconstructs the geometry of highly specular surfaces alongside the reflection of nearby objects.

that 3DGS-DR [39] performs better than GShader [13] in reconstructing the direct part of incident radiance from the environment, showing the superiority of surface-based deferred shading over volumetric rendering in PBR modeling of high-frequency reflections. Our method, with well-optimized geometry and consequent accurate incident radiance modeling, achieves satisfactory novel view synthesis of specular reflection on both synthetic and real-world scenes, as also indicated in Fig. 5.

# 4.4. Ablation Study

On a subset of our synthetic scenes, we validate the following key component of our method: (1) Normal prior guidance; (2) Joint geometry optimization from incident lighting; (3) ray-traced Indirect incident radiance; (4) Progressive learning; and (5) Depth-aware ray perturbation. The results are shown in Tab. 3. Our full method (Ours) achieves the highest scores, confirming the effectiveness of our method designs. Without the initial normal prior guidance (Ours w/o N.), the optimization process is prone to be trapped into local minima far away from the true underneath geometry of the reflective region. On the other hand, only relying on normal priors without further joint optimization for fine-tuning geometry (Ours w/o J.) also fails in reconstructing accurate geometry for physically-based highfrequency reflections. As discussed above, using only direct incident lighting modeling (Ours w/o I.) leads to baked-in indirect incident lighting and damages the quality of highfrequency components. The progressive learning scheme (Ours w/o P.) and depth-aware ray perturbation (Ours w/o **D**.) also further helps to faithfully reconstruct the scene.

#### 4.5. Applications

Our Gaussian point cloud representation with explicit geometry, material, and incident lighting facilitates various

Table 3. Ablation study with variants of our proposed method excluding: Normal prior guidance, Joint geometry optimization, Indirect incident lighting modeling, Progressive learning, and Depth-aware ray perturbation.  $\uparrow(\downarrow)$  means higher (lower) is better.

	Е	ntire Ima	ge	Reflective Region				
Method	<b>PSNR</b> ↑	SSIM↑	LPIPS↓	<b>PSNR</b> ↑	SSIM↑	LPIPS↓		
Ours w/o N.	26.70	0.885	0.149	19.80	0.913	0.094		
Ours w/o J.	26.37	0.878	0.154	19.52	0.907	0.100		
Ours w/o I.	28.49	0.905	0.130	22.19	0.935	0.074		
Ours w/o P.	29.26	0.910	0.118	23.16	0.940	0.062		
Ours w/o D.	29.75	0.914	0.114	23.88	0.944	0.056		
Ours	29.90	0.914	0.112	24.05	0.944	0.056		



Figure 6. Our explicit representation of geometry, material, and incident lighting in the Gaussian point cloud enables various editing applications. Insets have been brightened for clarity.

editing applications. As illustrated in Fig. 6, specular objects of interest can be faithfully captured as assets in the presence of unwanted reflections from nearby objects, enabling further usages such as relighting (column 1) and material editing (column 4). We can also manipulate the scene geometry such as deletion (column 2) and insertion (column 3), with specular inter-reflections adjusted accordingly.

# 5. Conclusion

We introduce SpecTRe-GS to model highly specular surfaces with inter-reflections, distinguished by its separate modeling of specular and rough surfaces, the efficient ray tracer, and a geometry-enhancing training strategy for fast and accurate specular inter-reflection rendering.

**Limitations.** We only model specular inter-reflections from rough surfaces to avoid multi-bounce path tracing, and we only trace one secondary ray for each pixel in the reflective region, approximating the specular reflection with an ideal mirror. Also, the monocular normal prior may fail in the existence of strong semantic ambiguity (such as mirrors with hidden borders), making our geometry fail to initialize.

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# SpecTRe-GS: Modeling Highly Specular Surfaces with Reflected Nearby Objects by Tracing Rays in 3D Gaussian Splatting

Supplementary Material

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In this supplementary material, we provide additional implementation details for SpecTRe-GS (Sec. 6), the creation details of synthetic and real-world data (Sec. 7), and further qualitative/quantitative results and experimental analyses (Sec. 8). The videos on the project page<sup>1</sup> showcase qualitative view interpolation and scene editing results.

## 6. Additional Implementation Details

# **6.1. Implementation of Ray Tracing**

The ray tracer described in Sec. 3.3 in the main paper is implemented in OptiX 7 [7] and integrated into the 3DGS framework with the PyOptiX package as the Python bindings for the OptiX host API. According to the OptiX 7 specification, the OptiX pipeline consists of user-programmable entry points (programs) for different stages in ray tracing, we implement ray tracing in the Gaussians point cloud with custom *ray-gen* and *any-hit* programs:

- we initialize ray origin and direction, set and read the perray payloads, evaluate responses of Gaussians, and aggregate the volumetric radiance in the *ray-gen* program;
- we calculate the precise hit point of the mesh-bounded Gaussians and store the hit information into the per-ray buffer in the *any-hit* program.

The programs are described in Proc. 1 and Proc. 2. In our implementation, we construct a max heap of size k = 256 to store the closest hits with the complexity of  $\mathcal{O}(N \log k)$ , where N is the total number of hits.

### 6.2. Alignment of Rasteriazion and Ray Tracing

We align the radiance aggregation process of our ray tracer to that of the rasterizer. We use the rasterizer in GOF [14] as GOF calculates the maximum response of Gaussians along the rays. However, GOF still uses projected center depths to sort Gaussians in volumetric rendering. Therefore, we deliberately calculate projected depths as  $t_{hit,i}$  in our ray tracer and use  $t_{hit,i}$  instead of  $t_{max,i}$  for the ordering in Eq. (1). We also use the same ray termination threshold of remaining transmittance  $T_{\rm min} = 0.001$  and max number of contributing Gaussians  $K_{\rm max} = 256$  for our rasterizer and ray tracer. This reduces the discrepancy between the rendered appearances of the same Gaussian point cloud by these two renderers, which would cause the inconsistency between the directly observed appearance of objects and their appearance through a highly specular surface.

Procedure 1: Ray-gen Program
<b>Input:</b> ray origin $o$ , ray direction $d$ , GAS handle $\mathcal{H}$ ,
Gaussians $\{\mathcal{G}_i\}$ , min transmittance $T_{\min}$ ,
min contribution $\alpha_{\min}$ , hit buffer size k, min
ray distance $t_{near}$ , max ray distance $t_{far}$
<b>Output:</b> ray incident radiance $I_{ind}$ , ray visibility $V_i$ ,
ray depth $D_{\rm ind}$
1 $I_{\text{ind}} \leftarrow (0,0,0);$
2 $V_{\mathrm{i}} \leftarrow 1;$
$ 3 \ D_{\mathrm{ind}} \leftarrow 0; $
4 $t_{\text{curr}} \leftarrow t_{\text{near}};$
5 while $t_{ m curr} < t_{ m far}$ and $V_{ m i} > T_{ m min}$ do
$6 \qquad c \leftarrow 0;$
7 $\mathcal{B} \leftarrow \operatorname{buffer}(k);$
8 setPayload( $\mathcal{B}, c$ );
9 traceRay( $\mathcal{H}, \boldsymbol{o} + t_{curr} \boldsymbol{d}, \boldsymbol{d}, k$ );
10 $\mathcal{B}, c \leftarrow \text{getPayload}();$
11 if $c = 0$ then
12   terminateRay();
13 end
14 $B \leftarrow \operatorname{sort}(B);$
15 for $(t_{hit}, i)$ in $\mathcal{B}$ do
16 $t_{\max}, \alpha_{\text{hit}} \leftarrow \operatorname{response}(\mu_i, s_i, q_i, o, d);$
17 If $\alpha_{\rm hit} > \alpha_{\rm min}$ then
$\begin{array}{c} 18 \\$
19 $I_{\text{ind}} \leftarrow I_{\text{ind}} + \alpha_{\text{hit}} V_i c_i;$
$\begin{array}{c c} 20 \\ 1 \\$
21 $V_i \leftarrow (1 - \alpha_{\rm hit})V_i;$
22 end
23   $t_{curr} \leftarrow t_{hit};$
24 end
25 end

The work was done during an internship in Huawei.

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<sup>&</sup>lt;sup>1</sup>https://spectre-gs.github.io/

Procedure 2: Any-hit Program

**Input:** ray origin *o*, ray direction *d*, Gaussians  $\{\mathcal{G}_i\}$ , hitted primitive index *i*, hit buffer  $\mathcal{B}$ , hit buffer size k, hit count c**Output:** in-place modified hit buffer  $\mathcal{B}$ , hit count c1  $t_{\text{hit}} \leftarrow \text{projectDepth}(\boldsymbol{\mu}_i, \boldsymbol{o}, \boldsymbol{d});$ 2  $h \leftarrow (t_{\text{hit}}, i);$ 3 if c = k then 4  $h_{\max} \leftarrow \mathcal{B}.popMax();$ 5 else  $h_{\max} \leftarrow (+\infty, -1));$ 6  $c \leftarrow c + 1;$ 7 8 end 9  $h_{\text{new}} \leftarrow \text{findCloser}(h_{\max}, h);$ 10  $\mathcal{B}$ .insert $(h_{new})$ ;

## 6.3. Training Details

During training, we use the same color reconstruction loss as commonly adopted in 3DGS-based methods [5]:

$$\mathcal{L}_{\rm c} = 0.8 \cdot \frac{1}{|I_{\rm GT}|} \sum ||I_{\rm GT} - I||_1 - 0.2 \cdot \text{SSIM}(I_{\rm GT}, I),$$
(14)

and we also apply this loss to  $I_{ss}$  in later training steps (>15k iterations) to encourage physics-based modeling of highly reflective regions.

We follow Eq. (1) to compute the mean depth of contributing Gaussians as the surface depth, instead of the depth of the "median" Gaussian in GOF [14], which we find is generally more noisy and inefficient in utilizing gradient signals. In the first 4k steps, we only rely on SH color modeling to quickly get a rough geometry initialization and low-frequency view-dependent radiance modeling.

Since the Fresnel reflectance is calculated from approximation (Eq. (4)), we detach  $\partial A_{\text{spec}}/\partial n$  and clip  $A_{\text{spec}}$  as  $\min(A_{\text{spec}}, 10F_0)$  to ensure numerical stability.

We only run StableNormal [12] once for all scenes and save the estimated normals as monocular normal priors.

## 6.4. Tone Mapping

Our method operates in linear color space as required by physically-based rendering. We assume the gammacorrected sRGB space of  $\gamma = 2.2$  is usually used in the input images, which is closer to human perception. Thus, we can convert the images into linear color space by inversely applying the gamma correction. We convert our results back to the commonly adopted gamma-corrected sRGB space with  $\gamma = 2.2$  prior to visualization or the computation of photometric losses and error metrics.

## 7. Data Creation Details

#### 7.1. Synthetic Scenes

We collect 6 synthetic scenes using the Blender Cycles engine [3]: HELMET, MARBLETABLE, VASE, POT, TOASTER, and MIRROR, as described in Sec. 4.2 in the main paper. We show example images of each scene in Tab. 4 and Tab. 5 of this document.

#### 7.2. Real-world Scenes

For real-world scenes, we use a hand-held iPhone 15 Pro and the "ProCam" app to take raw images with a linear camera response. We fix the white balance, focal length, exposure time, and ISO for all images in the same scene. We register the camera poses using COLMAP [8, 9] with SuperPoint [2] for feature extraction and LightGlue [6] for matching. After obtaining the captured raw images of the scene, we use a custom image signal processor (ISP) to process the raw image by, e.g., demosaicking, white balancing, transforming color space, and most importantly, applying a tone mapping with  $\gamma = 2.2$  to let the processed images satisfy our assumption of availability of linear space images. We resize the images to  $1440 \times 1080$  and remove the outof-focus background regions. The highly reflective regions are manually marked. By doing so, we collect 2 real-world scenes: REALBOWL and REALPOT. We show example images of each scene in Tab. 5 of this document.

# 8. Additional Results

## 8.1. Results with Varying Roughness

Our method is designed for perfect mirror reflections. Nevertheless, the inclusion of a low-frequency component gives it the ability to model rougher surfaces to some extent. Fig. 7 shows its results on the HELMET scene with varying roughness, from highly smooth ( $\rho = 0.05$ ) to medium rough ( $\rho = 0.3$ ). For each roughness value, we show the rendered image and the ground truth image in a test view, alongside the decomposition of specular component  $A_{\text{spec}}I_i \odot (1 - I_r)$  and low-frequency component  $I_{\text{diff}} \odot$  $(1 - I_r) + I_{rs} \odot I_r$ , expanded according to the modeling in Sec. 3.2 and soft mask  $I_r$  in Sec. 3.4. As the roughness increases, while direct specular reflections can be approximated by blurred environment maps, indirect specular reflections in the lower half of the helmet are mimicked by brighter  $I_{rs}$  with lower  $A_{\text{spec}}$  values.

# 8.2. Geometry Representation

As shown in Fig. 8, our method can better capture the planar surface in MARBLETABLE scene with most points well aligned to the object, benefitting from our normal prior guidance and joint optimization of incident radiance and geometry. Without accurate geometry optimization and inci-



Figure 7. As surface roughness increases, our method attributes more proportion of the scene appearance to low-frequency reflection instead of perfect mirror reflection.

dent radiance reconstruction, other methods tend to fit highfrequency view-dependent specular reflection with highfrequency floaters.

## 8.3. Qualitative Ablation Results

Fig. 9 shows the results of the ablated variants of our method mentioned in Sec. 4.4 in the same view as Fig. 4. When the monocular normal prior guidance is absent during early training stages (Ours w/o N.), the training loss terms tend to overemphasize color reconstruction fidelity in observed images, causing the scene representation to converge to local minima with geometry deviating from ground truth in highly specular regions (as shown by the translucent artifacts on the left side of the helmet in column 1, indicating incomplete underlying geometric reconstruction). Conversely, when relying solely on monocular normal priors without subsequent joint optimization to refine scene geometry (Ours w/o J.), the inherent inaccuracies and multi-view inconsistencies in monocular normal predictions prevent the reconstruction of precise geometry required for physics-based high-frequency reflection modeling (evidenced by the missing high-frequency details in the reflections on the helmet surface, as depicted in column 2). As previously discussed regarding physics-based rendering approaches, modeling only direct illumination (Ours w/o I.) leads to indirect lighting effects being baked into either SH color representations or diffuse albedo, thereby compromising high-frequency component quality (manifested as missing high-frequency details and ghosting artifacts in the lower helmet region due to inter-reflections, shown in column 3). The progressive learning scheme (Ours w/o P.) and depth-aware ray perturbation (Ours w/o D.) also significantly contribute to faithful reconstruction of view-dependent high-frequency specular reflections.

#### 8.4. Alignment of Rendering Methods

We analyze the consistency of rendering results from our rasterizer and ray tracer on the STUMP scene of the Mip-NeRF 360 dataset [1], which is a prerequisite for accurately evaluating indirect incident radiance. We show the rendered images and the corresponding PSNR scores of each renderer in Fig. 10, accompanied by the error map visualiza-



Figure 8. Visualization of the point cloud reconstructed by comparing methods [4, 5, 10, 13, 14]. Ours more faithfully captures the underlying geometry of reflective regions, while other methods disrupt their geometry to imitate highly specular reflections.



Figure 9. Qualitative ablation results with variants of our proposed method excluding: Normal prior guidance, Joint geometry optimization, Indirect incident lighting modeling, Progressive learning, and Depth-aware ray perturbation.



Figure 10. Rasterized and ray-traced results in our proposed method are highly consistent, which ensures accurate indirect incident radiance queries from the Gaussian point cloud shared by our rasterizer and ray tracer.

tion. The rendering results from those two renderers in our pipeline remain highly consistent, as indicated by the inconspicuous visual difference, the close PSNR scores, and the colors in the error map.

## **8.5.** More Quantitative Results

We show detailed quantitative results on each scene in Tab. 4 and Tab. 5 of this document. In general, our SpecTRe-GS consistently outperforms most compared methods on both synthetic scenes and real-world scenes, especially within reflective regions.

#### **8.6.** More Qualitative Results

We show additional qualitative comparisons with the baseline methods<sup>2</sup> on each scene in Fig. 11-14 of this document. For each scene, we show comprehensive visual comparison results from multiple test views. We provide videos of view interpolation results as attached files on the project page. Compared with baseline methods, our method gives more view-consistent renderings of high-frequency reflection, which better respects the geometry of the highly reflective surfaces. In addition, we provide videos of the scene editing results.

<sup>&</sup>lt;sup>2</sup>We show results of GShader\* for all scenes, 3DGS-DR\* for HELMET scene as their better performance indicated by quantitative evaluations.

Table 4. Quantitative comparison results with state-of-the-art methods on each of the 4 synthetic scenes (HELMET, MARBLETABLE, VASE, and POT). We show example images and the dataset splits of each scene in the leftmost column. We report the scores of PSNR, SSIM [11], and LPIPS [15] for entire images and within reflective regions. We mark the **best** and the <u>second best</u> results in each column.  $\uparrow (\downarrow)$  means higher (lower) is better.

		Entire Image			Reflective Region			
Scene	Method	PSNR↑	<b>SSIM</b> ↑	LPIPS↓	<b>PSNR</b> ↑	<b>SSIM</b> ↑	LPIPS↓	
Helmet	3DGS [5]	27.92	0.881	0.157	21.62	0.918	0.090	
(train: 201, test:100)	GOF [14]	28.28	<u>0.893</u>	0.130	21.62	0.918	0.086	
	GOF* [14]	27.15	0.887	0.145	20.28	0.912	0.100	
	3iGS [10]	<u>28.33</u>	0.883	0.152	22.06	0.919	0.088	
	GShader [4]	25.80	0.836	0.204	20.72	0.913	0.098	
	GShader* [4]	26.51	0.846	0.196	21.28	0.915	0.097	
	3DGS-DR [13]	26.32	0.841	0.233	20.76	0.914	0.098	
	3DGS-DR* [13]	27.15	0.845	0.226	22.36	0.927	<u>0.083</u>	
_	Ours	29.90	0.914	0.112	24.05	0.944	0.056	
MARBLETABLE	3DGS [5]	22.41	0.858	0.197	20.10	<u>0.889</u>	0.142	
(train: 233, test:123)	GOF [14]	23.59	<u>0.873</u>	0.177	19.77	<u>0.889</u>	0.137	
	GOF* [14]	24.14	0.870	0.187	19.71	0.884	0.150	
	3iGS [10]	24.42	0.865	0.184	20.09	0.880	0.145	
	GShader [4]	24.28	0.856	0.209	20.65	0.878	0.160	
	GShader* [4]	24.89	0.865	0.198	21.27	0.886	0.152	
	3DGS-DR [13]	25.37	0.857	0.223	22.02	0.882	0.164	
1 Carlos	3DGS-DR* [13]	22.51	0.837	0.239	19.63	0.866	0.180	
	Ours	26.89	0.875	<u>0.183</u>	22.38	0.890	<u>0.142</u>	
VASE	3DGS [5]	33.16	0.944	0.093	26.42	<u>0.975</u>	0.042	
(train: 201, test:100)	GOF [14]	33.28	<u>0.948</u>	<u>0.083</u>	26.36	<u>0.975</u>	0.040	
	GOF* [14]	32.72	0.945	0.087	25.32	0.973	0.045	
	3iGS [10]	33.02	0.943	0.091	26.60	<u>0.975</u>	0.042	
	GShader [4]	30.33	0.912	0.129	25.14	0.973	0.046	
	GShader* [4]	30.79	0.919	0.121	25.44	0.973	0.046	
	3DGS-DR [13]	31.35	0.914	0.149	25.86	0.973	0.046	
	3DGS-DR* [13]	30.94	0.912	0.152	25.10	0.971	0.049	
	Ours	33.14	0.949	0.076	27.20	0.982	0.027	
Рот	3DGS [5]	29.88	0.923	0.096	23.50	0.945	0.062	
(train: 201, test:100)	GOF [14]	29.71	0.921	0.093	23.41	0.943	<u>0.058</u>	
	GOF* [14]	29.04	0.919	0.105	22.22	0.940	0.071	
205	3iGS [10]	31.13	<u>0.928</u>	<u>0.090</u>	<u>23.88</u>	<u>0.947</u>	0.059	
	GShader [4]	29.37	0.913	0.116	22.53	0.942	0.068	
	GShader* [4]	29.53	0.915	0.114	22.86	0.943	0.066	
	3DGS-DR [13]	30.22	0.917	0.115	23.34	0.944	0.066	
	3DGS-DR* [13]	28.87	0.909	0.125	22.23	0.940	0.074	
	Ours	<u>30.30</u>	0.933	0.075	24.79	0.959	0.035	

Table 5. Quantitative comparison results with state-of-the-art methods on each of the 2 synthetic scenes (TOASTER and MIRROR) and 2 real-world scenes (REALBOWL, and REALPOT). We show example images and the dataset splits of each scene in the leftmost column. We report the scores of PSNR, SSIM [11], and LPIPS [15] for entire images and within reflective regions. We mark the **best** and the <u>second best</u> results in each column.  $\uparrow(\downarrow)$  means higher (lower) is better.

		Entire Image			Reflective Region		
Scene	Method	<b>PSNR</b> ↑	SSIM↑	LPIPS↓	<b>PSNR</b> ↑	<b>SSIM</b> ↑	LPIPS↓
TOASTER	3DGS [5]	26.26	0.914	0.123	18.77	<u>0.951</u>	0.060
(train: 201, test:100)	GOF [14]	26.34	0.924	0.103	18.74	<u>0.951</u>	0.060
	GOF* [14]	25.61	<u>0.918</u>	<u>0.115</u>	17.99	0.945	0.070
	3iGS [10]	<u>26.71</u>	0.914	0.120	<u>19.34</u>	<u>0.951</u>	0.056
	GShader [4]	25.51	0.897	0.146	18.16	0.944	0.070
	GShader* [4]	26.07	0.900	0.143	18.77	0.946	0.068
	3DGS-DR [13]	25.68	0.885	0.175	18.42	0.949	0.064
	3DGS-DR* [13]	25.97	0.871	0.199	18.95	0.947	0.069
	Ours	27.73	<u>0.918</u>	<u>0.115</u>	20.39	0.953	0.062
Mirror	3DGS [5]	26.65	0.938	0.120	18.65	<u>0.963</u>	0.072
(train: 201, test:100)	GOF [14]	26.65	0.941	0.112	18.37	0.962	0.074
	GOF* [14]	26.74	0.941	0.113	18.52	<u>0.963</u>	0.074
	3iGS [10]	<u>27.86</u>	<u>0.939</u>	0.115	<u>19.90</u>	0.964	<u>0.067</u>
	GShader [4]	24.61	0.913	0.156	17.52	0.961	0.075
	GShader* [4]	25.02	0.917	0.149	17.71	0.962	0.074
	3DGS-DR [13]	26.77	0.924	0.145	19.04	0.964	0.069
	3DGS-DR* [13]	26.40	0.920	0.152	18.83	0.963	0.075
	Ours	28.64	0.938	0.097	20.66	0.963	0.056
REALBOWL	Ours	<b>28.64</b> 25.75	0.938 0.832	<b>0.097</b> 0.212	<b>20.66</b> 20.73	0.963 0.967	<b>0.056</b>
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14]	<b>28.64</b> 25.75 <u>25.79</u>	0.938 0.832 <u>0.835</u>	0.097 0.212 <u>0.202</u>	<b>20.66</b> 20.73 20.71	0.963 0.967 0.966	0.056 0.041 <u>0.039</u>
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14]	<b>28.64</b> 25.75 <u>25.79</u> 25.59	0.938 0.832 <u>0.835</u> 0.834	0.097 0.212 <u>0.202</u> 0.205	<b>20.66</b> 20.73 20.71 19.81	0.963 0.967 0.966 0.965	0.056 0.041 <u>0.039</u> 0.043
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10]	<b>28.64</b> 25.75 <u>25.79</u> 25.59 25.34	0.938 0.832 <u>0.835</u> 0.834 0.819	0.097 0.212 0.202 0.205 0.216	20.66 20.73 20.71 19.81 <u>20.80</u>	0.963 0.967 0.966 0.965 0.967	0.056 0.041 <u>0.039</u> 0.043 0.040
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4]	<b>28.64</b> 25.75 <u>25.79</u> 25.59 25.34 24.76	0.938 0.832 0.835 0.834 0.819 0.817	0.097 0.212 0.202 0.205 0.216 0.240	20.66 20.73 20.71 19.81 <u>20.80</u> 19.68	0.963 0.967 0.966 0.965 0.967 0.966	0.056 0.041 0.039 0.043 0.040 0.045
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] GShader* [4]	<b>28.64</b> 25.75 <u>25.79</u> 25.59 25.34 24.76 24.82	0.938 0.832 0.835 0.834 0.819 0.817 0.819	0.097 0.212 0.202 0.205 0.216 0.240 0.239	20.66 20.73 20.71 19.81 20.80 19.68 19.82	0.963 0.967 0.966 0.965 0.967 0.966 0.966	0.056 0.041 0.039 0.043 0.040 0.045 0.045
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] GShader* [4] 3DGS-DR [13]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227	20.66 20.73 20.71 19.81 <u>20.80</u> 19.68 19.82 20.58	0.963 0.967 0.966 0.965 0.967 0.966 0.966 0.967	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.042
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] 3DGS-DR [13] 3DGS-DR* [13]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236	20.66 20.73 20.71 19.81 20.80 19.68 19.82 20.58 19.86	0.963 0.967 0.966 0.965 0.967 0.966 0.966 0.966 0.966	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.042 0.045
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] 3DGS-DR [13] 3DGS-DR* [13] Ours	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 25.48 26.16	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 0.839	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195	20.66 20.73 20.71 19.81 20.80 19.68 19.82 20.58 19.86 22.84	0.963 0.967 0.966 0.965 0.967 0.966 0.966 0.966 0.966 0.966 0.966 0.973	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.042 0.045 0.045 0.045 0.045
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] GShader* [4] 3DGS-DR [13] 3DGS-DR* [13] Ours 3DGS [5]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 26.16 23.89	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 0.839 0.814	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245	20.66 20.73 20.71 19.81 20.80 19.68 19.82 20.58 19.86 22.84 21.89	0.963 0.967 0.966 0.965 0.967 0.966 0.966 0.966 0.966 0.966 0.973 0.962	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045
REALBOWL (train: 120, test:18) Example 120 REALPOT (train: 121, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] 3DGS-DR [13] 3DGS-DR* [13] Ours 3DGS [5] GOF [14]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 26.16 23.89 23.94	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 <b>0.839</b> 0.814 <b>0.817</b>	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245 0.235	20.66 20.73 20.71 19.81 <u>20.80</u> 19.68 19.82 20.58 19.86 <b>22.84</b> <u>21.89</u> 21.78	0.963           0.967           0.966           0.965           0.967           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966           0.966	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.056 0.055
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] GShader* [4] 3DGS-DR [13] 3DGS-DR* [13] Ours 3DGS [5] GOF [14] GOF* [14]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 26.16 23.89 <u>23.94</u> 23.80	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 0.839 0.814 0.817 0.816	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245 0.245 0.245 0.240	20.66 20.73 20.71 19.81 <u>20.80</u> 19.68 19.82 20.58 19.86 <b>22.84</b> <u>21.89</u> 21.78 21.07	0.963 0.967 0.966 0.965 0.967 0.966 0.966 0.966 0.966 0.973 0.960 0.959	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.055 0.059
REALBOWL (train: 120, test:18) <b>Free Constitution</b> <b>REALPOT</b> (train: 121, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] GShader* [4] 3DGS-DR [13] 3DGS-DR* [13] Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 26.16 23.89 23.94 23.80 23.40	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 <b>0.839</b> 0.814 <b>0.817</b> <u>0.814</u> 0.817 <u>0.816</u> 0.799	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245 0.245 0.245 0.245 0.240 0.249	20.66 20.73 20.71 19.81 <u>20.80</u> 19.68 19.82 20.58 19.86 <b>22.84</b> <u>21.89</u> 21.78 21.07 21.63	0.963 0.967 0.966 0.965 0.966 0.966 0.966 0.966 0.966 0.973 0.960 0.959 0.960	0.056           0.041           0.039           0.043           0.040           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.045           0.056           0.055           0.059           0.055
REALBOWL (train: 120, test:18)	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] 3DGS-DR [13] 3DGS-DR* [13] Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 26.16 23.89 23.94 23.80 23.40 23.11	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 <b>0.839</b> 0.814 <b>0.817</b> <u>0.816</u> 0.799 0.802	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245 0.245 0.245 0.240 0.249 0.271	20.66 20.73 20.71 19.81 20.80 19.68 19.82 20.58 19.86 22.84 21.89 21.78 21.07 21.63 20.77	0.963           0.967           0.966           0.965           0.967           0.966           0.966           0.966           0.966           0.966           0.967           0.966           0.966           0.966           0.966           0.966           0.960           0.959           0.960           0.960	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.055 0.059 0.055 0.061
REALBOWL (train: 120, test:18)	Ours         3DGS [5]         GOF [14]         GOF* [14]         3iGS [10]         GShader [4]         GShader [4]         3DGS-DR [13]         3DGS-DR* [13]         Ours         3DGS [5]         GOF [14]         GOF* [14]         3iGS [10]         GShader [4]         GShader [4]	28.64         25.75         25.79         25.59         25.34         24.76         24.82         25.66         25.48         26.16         23.89         23.94         23.40         23.11         23.23	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 <b>0.839</b> 0.814 <b>0.817</b> <u>0.816</u> 0.799 0.802 0.806	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245 0.245 0.245 0.240 0.249 0.271 0.267	20.66 20.73 20.71 19.81 <u>20.80</u> 19.68 19.82 20.58 19.86 <b>22.84</b> <u>21.89</u> 21.78 21.07 21.63 20.77 20.89	0.963           0.967           0.966           0.965           0.967           0.966           0.966           0.966           0.966           0.966           0.967           0.966           0.967           0.966           0.967           0.966           0.967           0.966           0.960           0.959           0.960           0.961	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.045 0.045 0.045 0.056 0.055 0.059 0.055 0.061 0.060
REALBOWL (train: 120, test:18)Image: State of the state of	Ours         3DGS [5]         GOF [14]         GOF* [14]         3iGS [10]         GShader [4]         GShader* [4]         3DGS-DR [13]         3DGS-DR* [13]         Ours         3DGS [5]         GOF [14]         GOF* [14]         3iGS [10]         GShader [4]         GShader [4]         3DGS-DR [13]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 26.16 23.89 23.94 23.80 23.40 23.40 23.11 23.23 23.91	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 <b>0.839</b> 0.814 <b>0.817</b> <u>0.816</u> 0.799 0.802 0.806 <u>0.816</u>	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245 0.245 0.245 0.245 0.245 0.249 0.271 0.267 0.258	20.66 20.73 20.71 19.81 20.80 19.68 19.82 20.58 19.86 22.84 21.89 21.78 21.07 21.63 20.77 20.89 21.78	0.963           0.967           0.966           0.965           0.967           0.966           0.966           0.966           0.966           0.966           0.967           0.966           0.967           0.966           0.967           0.966           0.967           0.966           0.960           0.959           0.960           0.961           0.962	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.045 0.045 0.055 0.056 0.055 0.059 0.055 0.061 0.060 0.058
REALBOWL (train: 120, test:18)Image: State of the state of	Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] GShader [4] 3DGS-DR [13] 3DGS-DR* [13] Ours 3DGS [5] GOF [14] GOF* [14] 3iGS [10] GShader [4] GShader [4] 3DGS-DR [13] 3DGS-DR* [13]	28.64 25.75 25.79 25.59 25.34 24.76 24.82 25.66 25.48 26.16 23.89 23.94 23.80 23.40 23.11 23.23 23.91 23.71	0.938 0.832 0.835 0.834 0.819 0.817 0.819 0.832 0.830 <b>0.839</b> 0.814 <b>0.817</b> <u>0.816</u> 0.799 0.802 0.806 <u>0.816</u> 0.815	0.097 0.212 0.202 0.205 0.216 0.240 0.239 0.227 0.236 0.195 0.245 0.245 0.245 0.240 0.249 0.271 0.267 0.258 0.266	20.66 20.73 20.71 19.81 <u>20.80</u> 19.68 19.82 20.58 19.86 <b>22.84</b> <u>21.89</u> 21.78 21.07 21.63 20.77 20.89 21.78 20.90	0.963           0.967           0.966           0.965           0.967           0.966           0.966           0.966           0.966           0.966           0.967           0.966           0.967           0.966           0.967           0.966           0.967           0.966           0.967           0.960           0.959           0.960           0.961           0.962           0.961	0.056 0.041 0.039 0.043 0.040 0.045 0.045 0.045 0.045 0.045 0.045 0.055 0.059 0.055 0.059 0.055 0.061 0.060 0.058 0.064



Figure 11. Comparison with state-of-the-art methods on two synthetic scenes: HELMET and MARBLETABLE.



Figure 12. Comparison with state-of-the-art methods on two synthetic scenes: VASE and POT.



Figure 13. Comparison with state-of-the-art methods on two synthetic scenes: TOASTER and MIRROR.



Ground Truth

Ours

3DGS-DR

Figure 14. Comparison with state-of-the-art methods on two real-world scenes: REALBOWL and REALPOT.

GShader

3iGS

GOF

3DGS

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